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## PREDICTIONS OF PERFORMANCE IN CAREER EDUCATION

*M. R. Novick  
P. K. Jones  
N. S. Cole*

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P. O. BOX 168, IOWA CITY, IOWA 52240



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## ABSTRACT

Prediction weights for educational programs in 22 vocational and technical fields are provided using ability scores from The American College Testing Program (ACT) Career Planning Profile and a Bayesian regression theory due to D. V. Lindley as developed into an operational method by Jackson, Novick, and Thayer. The criterion variable studied was first-semester grade point average. Each vocational-technical program analyzed was represented by several institutions, and the usual least-squares regression weights for each institution were replaced by Bayesian weights which used both the direct information on that institution and the collateral information present in the other institutions offering that program. Very satisfactory predictions were obtained in 18 of the 22 programs: Business and Marketing, Dental Assisting, Nursing—Registered, Nursing—Practical, Other Health, Accounting, Business Administration (4-year transfer), Computer Programming, Data Processing, Secretarial Science, Electrical Engineering Technology, Science (4-year transfer), Other Technical, Auto Mechanics, Drafting, Machine Work, Other Trades, and Police Science. Largely because of a lack of sufficient data and the heterogeneity of the programs, predictions in four fields were not judged to be satisfactory: Agriculture, Cosmetology, Social Science (4-year transfer), and Arts and Humanities (4-year transfer). A detailed discussion of the generality of the  $m$  group regression model is provided.



# PREDICTIONS OF PERFORMANCE IN CAREER EDUCATION

Melvin R. Novick  
Paul K. Jones  
Nancy S. Cole

## INTRODUCTION

The prediction of performance in career education is by no means a simple problem. Each institution provides numerous diverse programs in which the enrollment in any one program is often small. An example of some typical numbers of enrolled students in several programs at a number of institutions is given in Table 1. The problem is then to predict performance in the diverse programs at many different institutions with only the minimal information available at any one institution in a particular program.

As can easily be seen from Table 1, the sample sizes for a particular program in a single institution are too small for the use of the usual least-squares procedures. Those procedures are subject to serious sampling variability in samples of such sizes.

It is common in 4-year colleges to pool information across all the students in a college, and because of the similarity of most freshman courses within a college, such a procedure is often successful. However, in career education, the diversity across programs within institutions is tremendous. For example, it is not feasible to combine Auto Mechanics students with those in Computer Programming. Also, even like-named programs across institutions may vary in content and level, although the diversity is commonly less than that across programs; therefore, simple pooling for a program across institutions is not practical. Consequently, a method is needed which uses the information from like-named programs at other institutions to compute predictions at a single institution while at the same time allowing for some differences in content and standards across institutions.

A procedure which allows the use both of the unique information from a program in a single institution and the *collateral information* from similar programs in other institutions is a Bayesian *m* group regression method developed by Jackson, Novick, and Thayer (1971) from a theory described by Lindley and Smith (1972). Novick, Jackson, Thayer, and Cole (1972) validated the Bayesian procedure in a group of 2-year colleges and found that the procedure yielded more efficient predictions than within-college least-squares weights in a situation in which there was enough diversity across colleges to preclude the simple pooling of data across colleges. When applied to the problem of prediction in career education, the Bayesian procedure provides for simultaneous estimation of prediction weights for like-named programs in different colleges. Thus, data such as that described in Table 1 can be used, for example, to provide predictions for students entering Institution 1 and Program B by simultaneously using the information on Program B in Institutions 2, 3, 6, 8, 9, 11. A student enrolling in Institution 1 can, therefore, be presented with a set of predictions for Pro-

TABLE 1

An Example of Typical Enrollments  
by Program and by Institution

| Insti-<br>tution | Programs |    |    |    |    |    |    |    |    |
|------------------|----------|----|----|----|----|----|----|----|----|
|                  | A        | B  | C  | D  | E  | F  | G  | H  | I  |
| 1                | 0        | 16 | 16 | 0  | 12 | 0  | 0  | 6  | 22 |
| 2                | 8        | 26 | 15 | 0  | 0  | 7  | 21 | 42 | 0  |
| 3                | 46       | 38 | 0  | 53 | 0  | 38 | 86 | 0  | 0  |
| 4                | 0        | 0  | 15 | 0  | 18 | 0  | 32 | 13 | 0  |
| 5                | 0        | 0  | 21 | 0  | 33 | 12 | 0  | 0  | 9  |
| 6                | 14       | 28 | 0  | 15 | 0  | 0  | 0  | 31 | 0  |
| 7                | 9        | 0  | 12 | 0  | 0  | 18 | 0  | 23 | 0  |
| 8                | 0        | 15 | 0  | 27 | 31 | 0  | 18 | 0  | 0  |
| 9                | 32       | 16 | 11 | 0  | 0  | 0  | 0  | 0  | 34 |
| 10               | 21       | 0  | 9  | 18 | 0  | 0  | 0  | 24 | 0  |
| 11               | 0        | 47 | 53 | 0  | 43 | 51 | 28 | 0  | 42 |
| 12               | 10       | 0  | 14 | 0  | 9  | 0  | 21 | 0  | 12 |

grams B, C, E, H, and I; and the accuracy of these predictions will have been enhanced by experience gained at the other institutions.

The purpose of the paper is to apply this Bayesian procedure to prediction of course performance in several career education programs at a number of

institutions using measures from the ACT Career Planning Program (CPP) as predictors. We examine the working details of the procedure, the quality of the predictions obtained; and the differences between various models which might be considered for prediction in career education.

## Method

Conducting effective Bayesian  $m$  group regression analysis requires a number of steps in which the available information is summarized, examined, refined, and prepared for the final analysis. To this end, a resource person with substantive background in education, a person with substantial computer experience, and a person thoroughly acquainted with Bayesian  $m$  group regression is required. Of course, all of these roles may be played by the same individual, but it is essential that all these skills are present. A detailed discussion of the technical-computational problems encountered in this study is given by Jones and Novick (1972) and will, therefore, not be discussed here.

The predictors used consisted of the seven ability scales of the ACT Career Planning Profile. These are given in Table 2.

**TABLE 2**  
**CPP Scales**

1. Mechanical Reasoning
2. Nonverbal Reasoning
3. Clerical Skills
4. Numerical Computation
5. Mathematical Usage
6. Space Relations
7. Reading Skills

Data were gathered in 1970 on over 10,000 entering students from over 60 institutions offering post-

secondary vocational-technical educational programs. The criteria measures were collected after the completion of one term in the program. The data sources were edited to ensure complete information on each scale for each individual.

Prediction of grades was performed in the 2-year colleges and vocational-technical schools for 22 educational programs or clusters of programs listed in Table 3. For most programs, vocational-technical course grades were employed as the criterion measure. However, academic course grades were considered to be the relevant criterion for programs leading to transfer to 4-year academic institutions.

**TABLE 3**

**Programs for Which Predictions  
Were Provided**

1. Agriculture
2. Business and Marketing
3. Dental Assisting
4. Nursing—Registered
5. Nursing—Practical
6. Other Health
7. Accounting
8. Business Administration (4-year transfer)
9. Computer Programming
10. Data Processing
11. Secretarial Science
12. Electrical Engineering Technology
13. Science (4-year transfer)
14. Other Technical
15. Auto Mechanics
16. Drafting
17. Machine Work
18. Other Trades
19. Cosmetology
20. Police Science
21. Social Science (4-year transfer)
22. Arts and Humanities (4-year transfer)



Two criteria were employed in selecting these programs. First, an adequate number of institutions and students had to be available for a program. Second, where programs were combined, it was necessary that the combination represent a rational grouping of fields of study. The purpose of the grouping was to reduce heterogeneity among schools as much as possible.

Variable selection was aided by reference to *Career Planning Profile National Norms for Vocational-Technical Students beyond High School* (The American College Testing Program, 1971) in which subsets of the ability measures of the CPP which would perform best in prediction were suggested. An attempt was made to choose for each program a set of variables that would be reasonably effective for all institutions offering that program. This approach differs from the usual approach which attempts a rote

maximization of a multiple correlation coefficient (R) for each institution, subject only to some limitation on the number of predictors used. For sample sizes of the magnitude encountered in the present study, reliance upon the estimated R within institution would result largely in capitalizing upon chance.

Accordingly, the field of seven predictors was reduced to combinations of one, two, or three variables at a time. Frequently, it was possible after several preliminary analyses to eliminate unsuitable variables (or unsuitable combinations of variables) from further consideration. In programs requiring some skill in Numerical Computation or Mathematical Usage, it was often possible to surmise which of these two skills would be more relevant to that program. Ordinarily, it did not prove useful to use both Numerical Computation and Mathematical Usage in the same prediction equation.

## Results and Discussion

The program involving Data Processing students clearly illustrates key points of the Bayesian method; hence, the analysis for that program is discussed here in some detail. Preliminary least-squares analyses together with consultation with the resource person resulted in the selection of Numerical Computation and Reading Skills (Variables 4 and 7) as predictors for the Data Processing program. Table 4 reports the regression weights and residual variance estimates for each of the 18 institutions offering this program. The classical Model II estimates represent a rough guess at the final Bayesian solution: Inspection by the reader will reveal that they tend to be closer to the final Bayesian estimates than the least-squares estimates. These classical Model II estimates are a weighted average of the least-squares values and the generalized weight values, just as the Bayesian estimates tend to be (albeit in a slightly different and more satisfactory mathematical form). The correspondence becomes less exact when several predictors are involved, but still the relationship is a usefully descriptive one for our purposes.

The exact Bayesian weights are obtained as the solution to an elaborate system of nonlinear equations, the *Lindley equations*. The least-squares estimates provide one set of starting points for the Bayesian solution while the classical Model II estimates provide another for the Bayesian regres-

sion computer program. By using both the least-squares and classical Model II regression solutions as starting values, a check on the convergence of the solution is obtained.

A generalized weight equation

$$\hat{Y} = .025X_4 + .035X_7 - .540$$

provides the appropriate prediction for students in a Data Processing program offered by an institution on which no past records are available. These weights are provided by the full Bayesian analysis. Roughly, the individual regression weights are the average of the corresponding weights across institutions. The intercept, however, is adjusted more carefully.

Next, note how the least-squares estimates tend to be "pulled-in" toward the generalized weights. As a consequence, the three negative weights on Variable 4 (Institutions 3, 9, and 10) have been eliminated. Similarly, the negative weights on Variable 7 (Institutions 4 and 7) have disappeared. Also, the residual variance estimates move toward an average value.

The greatest variation across institutions for the Bayesian estimate occurs for the intercept. The slopes tend to cluster about the generalized weight equation value, but this does not hold for the intercept. This is probably due to two reasons. First, the average GPA probably differs from institution to

TABLE 4

Regression Weights<sup>a</sup> and Residual Variances for Least-Squares, Classical Model II, and Bayesian Values for the Data Processing Program

| Insti-<br>tution | N  | Least-Squares Values |                 |                 |              | Classical Model II Values |                 |                 |              | Bayesian Values   |                   |                   |                | R     |
|------------------|----|----------------------|-----------------|-----------------|--------------|---------------------------|-----------------|-----------------|--------------|-------------------|-------------------|-------------------|----------------|-------|
|                  |    | $\hat{\beta}_0$      | $\hat{\beta}_4$ | $\hat{\beta}_7$ | $\hat{\phi}$ | $\hat{\beta}_0$           | $\hat{\beta}_4$ | $\hat{\beta}_7$ | $\hat{\phi}$ | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{\phi}$ |       |
| 1                | 12 | -1.825               | .041            | .052            | .8000        | -1.203                    | .034            | .047            | .2015        | -.382             | .028              | .034              | .4715          | .5082 |
| 2                | 12 | -3.024               | .096            | .039            | .5620        | -.335                     | .032            | .041            | .5443        | .006              | .029              | .032              | .4788          | .5015 |
| 3                | 14 | 2.698                | -.012           | .014            | .3101        | 1.176                     | .008            | .024            | .3932        | .495              | .019              | .025              | .4760          | .5016 |
| 4                | 18 | 1.774                | .019            | -.003           | .5991        | .212                      | .022            | .022            | .5701        | .072              | .020              | .027              | .4801          | .4977 |
| 5                | 12 | -.694                | .024            | .042            | .2660        | -.699                     | .025            | .042            | .3718        | -.528             | .027              | .036              | .4735          | .5081 |
| 6                | 15 | 1.020                | .005            | .034            | .6349        | -1.126                    | .022            | .038            | .5857        | -.151             | .027              | .032              | .4788          | .5028 |
| 7                | 19 | 2.558                | .013            | -.005           | .5528        | .445                      | .020            | .024            | .5429        | .040              | .022              | .028              | .4794          | .4979 |
| 8                | 10 | -2.332               | .020            | .056            | .3885        | -1.990                    | .023            | .046            | .4579        | -1.144            | .018              | .041              | .4765          | .5054 |
| 9                | 10 | -1.072               | -.061           | .014            | .3493        | -.845                     | .003            | .063            | .4360        | -.699             | .023              | .039              | .4787          | .5034 |
| 10               | 10 | -.677                | -.004           | .067            | .2146        | -.812                     | .010            | .054            | .3486        | -.696             | .022              | .039              | .4747          | .5066 |
| 11               | 30 | -2.215               | .052            | .042            | .1039        | -1.262                    | .034            | .042            | .8663        | -.881             | .031              | .038              | .4963          | .4860 |
| 12               | 35 | -1.465               | .049            | .035            | .4520        | -1.214                    | .042            | .038            | .4687        | -.857             | .035              | .037              | .4757          | .5107 |
| 13               | 28 | -1.173               | .042            | .027            | .8188        | -1.127                    | .033            | .035            | .7231        | -.873             | .028              | .036              | .4875          | .4966 |
| 14               | 50 | -1.312               | .017            | .058            | .6559        | -1.179                    | .020            | .052            | .6308        | -1.004            | .026              | .043              | .4872          | .5009 |
| 15               | 12 | -2.760               | .075            | .026            | .4087        | -1.414                    | .040            | .036            | .4627        | -.757             | .028              | .036              | .4766          | .5044 |
| 16               | 17 | -.009                | .008            | .034            | .5936        | -.952                     | .021            | .039            | .5659        | -.661             | .020              | .035              | .4784          | .5024 |
| 17               | 37 | -1.275               | .016            | .058            | .7797        | -1.059                    | .019            | .050            | .7132        | -.790             | .023              | .041              | .4898          | .4935 |
| 18               | 17 | -2.544               | .042            | .047            | .4738        | -1.914                    | .033            | .044            | .4941        | -.908             | .025              | .037              | .4767          | .5045 |

<sup>a</sup> $\beta_0$  Intercept

$\beta_4$  Weight for Variable 4 (Numerical Computation)

$\beta_7$  Weight for Variable 7 (Reading Skills)

$\phi$  Residual Variance

institution according to local grading practices. Second, the fact that the predictor variables have an approximate mean of 50 and a standard deviation of 10 will imply that the y-intercept will vary substantially despite only small changes in the slopes.

In addition, Table 4 reports the multiple correlation coefficient (R) for the Bayesian regression estimates. Calculations we made used the formula

$$R^2 = 1 - \frac{\phi}{\phi_0}$$

where  $\phi$  = Bayesian estimate of the residual variance using all predictors and  $\phi_0$  = Bayesian estimate of the residual variance using no predictors. It is important to emphasize that both the estimates  $\phi$  and  $\phi_0$  depend upon the same set of institutions. Since these

estimates are regressed for each institution within the program, the estimates of multiple Rs tend to be similar within the program. It should be noted that the above estimate of  $R^2$  is not a true Bayesian estimate but only a crude classical approximation and, hence, subject to the usual aberrations of classical estimation in Model II (a negative estimate is possible).

The most important statistics for each of the 22 vocational-technical programs are contained in Tables 5-26. In these tables, the institution sizes, regression weights, residual-variance estimates, and multiple Rs are given. Table 5 reports the generalized weight equations by program and Table 6 lists the predictor variables used for each program. Tables 7-28 contained in the Appendix give the specific Bayesian weights for each school on a program-by-program basis.

**TABLE 5**  
**Generalized Regression Coefficients for CPP Predictions of GPA**  
**by Vocational-Technical Program**

| Program | Number of<br>Institutions | Total No.<br>Students | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_2$ | $\tilde{\beta}_3$ | $\tilde{\beta}_4$ | $\tilde{\beta}_5$ | $\tilde{\beta}_6$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|---------|---------------------------|-----------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------|----------------|
| 1       | 13                        | 328                   | 1.300             | ---               | ---               | ---               | ---               | ---               | ---               | .027              | .1726       | .4339          |
| 2       | 12                        | 199                   | -.782             | ---               | ---               | ---               | .026              | ---               | ---               | .038              | .6580       | .3298          |
| 3       | 12                        | 307                   | .021              | ---               | ---               | ---               | .019              | ---               | ---               | .033              | .5775       | .3185          |
| 4       | 18                        | 583                   | .656              | ---               | ---               | ---               | .009              | ---               | ---               | .025              | .3483       | .4480          |
| 5       | 19                        | 475                   | .611              | ---               | ---               | ---               | .012              | ---               | ---               | .034              | .5126       | .2918          |
| 6       | 16                        | 529                   | .213              | ---               | ---               | ---               | .016              | ---               | ---               | .031              | .5002       | .3774          |
| 7       | 14                        | 291                   | .147              | ---               | ---               | ---               | .021              | ---               | ---               | .027              | .5216       | .3989          |
| 8       | 12                        | 306                   | .468              | ---               | ---               | ---               | .016              | ---               | ---               | .020              | .3268       | .4077          |
| 9       | 12                        | 258                   | -.401             | ---               | ---               | .020              | ---               | .035              | ---               | ---               | .4472       | .5414          |
| 10      | 18                        | 358                   | -.540             | ---               | ---               | ---               | .025              | ---               | ---               | .035              | .5019       | .4797          |
| 11      | 26                        | 914                   | .148              | ---               | ---               | ---               | .020              | ---               | ---               | .029              | .4646       | .4853          |
| 12      | 27                        | 824                   | -.484             | .013              | ---               | ---               | ---               | .031              | ---               | .012              | .4463       | .6060          |
| 13      | 10                        | 235                   | .526              | ---               | ---               | ---               | ---               | .022              | ---               | .011              | .4525       | .4493          |
| 14      | 19                        | 369                   | .966              | ---               | ---               | ---               | ---               | .031              | ---               | ---               | .3738       | .4449          |
| 15      | 20                        | 764                   | .503              | .014              | ---               | ---               | .013              | ---               | ---               | .014              | .4165       | .4360          |
| 16      | 17                        | 428                   | -.341             | .025              | ---               | ---               | .017              | ---               | ---               | .012              | .4470       | .5124          |
| 17      | 10                        | 163                   | -.336             | .020              | ---               | ---               | .037              | ---               | ---               | ---               | .5930       | .3820          |
| 18      | 24                        | 1398                  | .779              | .016              | ---               | ---               | .009              | ---               | ---               | .010              | .3764       | .4896          |
| 19      | 9                         | 163                   | 1.519             | ---               | ---               | ---               | ---               | ---               | ---               | .026              | .4551       | .2034          |
| 20      | 8                         | 209                   | .736              | .013              | ---               | ---               | ---               | ---               | ---               | .023              | .4250       | .4674          |
| 21      | 11*                       | 419                   | 1.430             | ---               | ---               | ---               | ---               | ---               | ---               | .020              | .1421       | .5490          |
| 22      | 6*                        | 326                   | 1.430             | ---               | ---               | ---               | ---               | ---               | ---               | .020              | .1421       | .5490          |

\*Programs 21 and 22 were combined to calculate the generalized regression coefficients.

TABLE 6

List of Variables Used by  
Vocational-Technical Program

1. Agriculture:  
Reading Skills
2. Business and Marketing:  
Numerical Computation, Reading Skills
3. Dental Assisting:  
Numerical Computation, Reading Skills
4. Nursing—Registered:  
Numerical Computation, Reading Skills
5. Nursing—Practical:  
Numerical Computation, Reading Skills
6. Other Health:  
Numerical Computation, Reading Skills
7. Accounting:  
Numerical Computation, Reading Skills
8. Business Administration (4-year transfer):  
Numerical Computation, Reading Skills
9. Computer Programming:  
Clerical Skills, Mathematical Usage
10. Data Processing:  
Numerical Computation, Reading Skills
11. Secretarial Science:  
Numerical Computation, Reading Skills
12. Electrical Engineering Technology:  
Mechanical Reasoning, Mathematical Usage,  
Reading Skills
13. Science (4-year transfer):  
Mathematical Usage, Reading Skills
14. Other Technical:  
Mathematical Usage
15. Auto Mechanics:  
Mechanical Reasoning, Numerical Computation,  
Reading Skills
16. Drafting:  
Mechanical Reasoning, Numerical Computation,  
Reading Skills
17. Machine Work:  
Mechanical Reasoning, Numerical Computation
18. Other Trades:  
Mechanical Reasoning, Numerical Computation,  
Reading Skills
19. Cosmetology:  
Reading Skills
20. Police Science:  
Mechanical Reasoning, Reading Skills
21. Social Science (4-year transfer):  
Reading Skills
22. Arts and Humanities (4-year transfer):  
Reading Skills

A full discussion of the theory of  $m$  group regression is given by Lindley and Smith (1972) and of the method by Jackson, Novick, and Thayer (1971) and, therefore, this will not be repeated here. However, it might be useful to discuss certain features of the model in greater depth than in previous papers; in particular, the assumptions underlying the model and how the model, in its generality, subsumes special cases considered by classical statistics.

First, an assumption of exchangeability is required for the analysis and must be emphasized here. The theory demands that our prior information be such that we not have (substantial) information to distinguish one course from another. This seems reasonable if all of our groups consist of students in Data Processing courses in various institutions, but it would not be reasonable if we also included in the analysis some Auto Mechanics groups. This does not imply that we believe, *a priori*, that all of the groups are the same, only that they are similar and that we do not have substantial prior information to differentiate them. One way of helping to justify the exchangeability assumption is to restrict the analysis to a single sex for some programs. For example, in the Nursing—Registered program, we used data only from female students. Prior experience suggests that somewhat different predictions are required for males; and thus, to the extent that some groups might have a higher percentage of males, they would not be exchangeable with the other groups. The effectiveness of this restriction to a single sex was demonstrated in the Novick, Jackson, Thayer, and Cole (1972) cross-validation.

When confronted with a problem of  $m$  group regression and, for the moment, putting aside the Bayesian solution, one is generally faced with the problem of selecting one of several possible models each requiring a restrictive assumption with regard to the data. Let us consider four such possible models and their relative attractiveness.

*Pooled Data within Institution*

It has been common in higher education to pool all data within an institution for prediction of college performance. In traditional 4-year colleges, such pooling is reasonable because of the similarity of courses taken by all freshman students. However, in career education, there is much greater diversity in

the courses included in different programs. Thus, pooling data from very dissimilar programs is not a feasible approach in career education, and such pooling would result in very poor predictions. Even if such pooling within institution were reasonable, it should be noted that within-institution pooling is a special case of a Bayesian  $m$  group regression on programs within institution. When the variance of regression coefficients across programs in such an analysis is very small, this Bayesian procedure reduces to the pooled-data within-institution model.

#### *Within-Program Group Least Squares*

Each program within an institution may be considered separately; and within-program, within-institution least-squares regression lines may be computed. In the present situation, this is probably the model that schools working their own would need to use because they would not have information on other schools. However, the samples are usually so small as to make within-group least squares infeasible. Even if information from other institutions were available to them, this would be the appropriate model for use if the various programs were, in fact, very dissimilar. It turns out that this model, also, is a special case of the Bayesian  $m$  group model; and results comparable to within-group least squares will be given by  $m$  group Bayesian regression when the data, in their entirety, support the assumption of a very large variance of the various regression coefficients between schools.

#### *Pooled Data for Programs across Institutions*

The third possible model goes to the other extreme and assumes there are no differences of the various like-named programs at different institutions and, thus, all of the data for a program are pooled and a single regression line is computed. It seems clear to us from the data in Table 4 and the other similar tables generated in this study together with general knowledge about the field of career education and the results obtained by Novick, Jackson, Thayer, and Cole (1972) that this model cannot be taken seriously in this application. However, we note that the pooled program data model is a special case of the Bayesian  $m$  group regression model, and corresponding estimates will be generated in the (unlikely) event that the variances across groups of *all* the regression coefficients are zero.

#### *Equal-Slopes Unequal-Intercepts*

If one is forced into a prior commitment to a simple model, this is probably the most realistic one of the four we discuss. We do not believe that the same slopes should be used for all schools, but we probably will do reasonably well as long as we allow the intercepts to vary. The weakness of this model is that it does least well when we have a school for which we have much data and the data indicate that this school, in fact, requires a different slope. Again, the Bayesian  $m$  group regression model includes this model as a special case, but if the data suggest that one or more schools have different slopes, the Bayesian solution will move in that direction for those schools.

It is possible to consider other more restrictive models, but this is no longer necessary. In fact, the Bayesian model incorporates a wide range of restrictive models as special cases and moves in the direction of one of these models as the data suggest the relevance of the particular model.

The price one pays for the generality of the Bayesian model is its complexity, the relative computational difficulty of getting out numerical solutions, and the care that is required in specifying some prior parameters. We feel, however, that the success of the method justifies the energy that has been spent developing and implementing it, and that those who are prepared to devote a substantial investment of time to the study of the method will have mastered a powerful tool. On the other hand, the computational difficulties involved in its application will probably restrict its usefulness to large-scale studies such as the one reported herein.

In the case of career education, the data presented here strongly suggest that the general Bayesian  $m$  group regression model will provide more efficient predictions of performance than possible with a simpler more restrictive model. This is not to say that one should routinely use the Bayesian  $m$  group regression or that it will be advantageous in all situations. If there is strong prior belief that a simpler model will be satisfactory in a situation, that model should certainly be used, subject to the understanding that if the data contradict the model, the model will be abandoned. However, for the prediction of performance in multiple diverse career-education programs at many institutions with only small numbers available in any one program within a single institution, the complexities of the Bayesian system appear to be necessary to provide satisfactory prediction.

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## APPENDIX

Tables 7-28 contain the specific Bayesian prediction weights for the various institutions providing data for the remaining 21 programs. The same numbers in the various tables do not generally signify the same institutions. The second column ( $n$ ) gives the within-school sample size. The next column ( $\tilde{\beta}_0$ ) gives the Bayesian estimate of the intercepts. The next one, two, or three columns give the Bayesian estimates of the regression coefficients for the variables used in prediction. For example, in Table 8, the Variables 4 (Numerical Computation) and 7 (Reading Skills) are used. The next column, headed  $\tilde{R}$ , gives an estimate of the true correlation between the predictor composite and criterion, and the final column gives an estimate of the residual variance.

TABLE 7

Regression Coefficients and Residual Variances  
for CPP Predictions of GPA for Institutions  
by Vocational-Technical Program

## Agriculture

| Institution | N   | $\tilde{\beta}_0$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|-----|-------------------|-------------------|-------------|----------------|
| 1           | 37  | 1.980             | .022              | .0989       | .4457          |
| 2           | 10  | 1.242             | .028              | .1811       | .4314          |
| 3           | 18  | 1.995             | .026              | .2037       | .4257          |
| 4           | 13  | 1.329             | .027              | .1905       | .4287          |
| 5           | 17  | 1.889             | .027              | .1802       | .4326          |
| 6           | 13  | .576              | .029              | .1568       | .4370          |
| 7           | 22  | 1.460             | .028              | .1777       | .4332          |
| 8           | 16  | .977              | .029              | .1902       | .4289          |
| 9           | 115 | .238              | .032              | .0911       | .4553          |
| 10          | 14  | 1.171             | .027              | .1734       | .4324          |
| 11          | 13  | 1.568             | .027              | .1846       | .4311          |
| 12          | 27  | 1.091             | .028              | .1805       | .4313          |
| 13          | 13  | 1.388             | .028              | .1889       | .4297          |

TABLE 8

## Business and Marketing

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 36 | .334              | .017              | .027              | .6410       | .3436          |
| 2           | 10 | -.630             | .026              | .030              | .6592       | .3275          |
| 3           | 11 | -1.416            | .031              | .036              | .6585       | .3302          |
| 4           | 16 | -1.684            | .029              | .063              | .6674       | .3269          |
| 5           | 18 | -1.238            | .027              | .048              | .6631       | .3253          |
| 6           | 11 | .843              | .021              | .021              | .6552       | .3326          |
| 7           | 18 | -.814             | .025              | .040              | .6560       | .3300          |
| 8           | 21 | -.865             | .027              | .037              | .6593       | .3272          |
| 9           | 10 | -1.222            | .029              | .043              | .6596       | .3281          |
| 10          | 11 | -.954             | .029              | .038              | .6588       | .3294          |
| 11          | 20 | -1.431            | .030              | .046              | .6612       | .3268          |
| 12          | 17 | -.308             | .025              | .023              | .6556       | .3303          |

TABLE 9

## Dental Assisting

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 19 | .620              | .005              | .033              | .5605       | .3155          |
| 2           | 33 | -1.520            | .027              | .036              | .5008       | .3198          |
| 3           | 21 | .314              | .016              | .032              | .5388       | .3316          |
| 4           | 14 | -.561             | .033              | .033              | .5602       | .3181          |
| 5           | 33 | .150              | .021              | .032              | .5638       | .3131          |
| 6           | 11 | 1.356             | .007              | .030              | .5556       | .3190          |
| 7           | 45 | -.837             | .019              | .039              | .5616       | .3164          |
| 8           | 15 | .862              | .003              | .032              | .5552       | .3189          |
| 9           | 16 | -.199             | .024              | .032              | .5546       | .3192          |
| 10          | 40 | -.120             | .021              | .034              | .5670       | .3128          |
| 11          | 42 | .523              | .031              | .027              | .5546       | .3215          |
| 12          | 18 | -.332             | .021              | .033              | .5603       | .3162          |

TABLE 10

## Nursing—Registered

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 17 | .460              | .008              | .031              | .3386       | .4550          |
| 2           | 55 | -.521             | .009              | .043              | .3465       | .4544          |
| 3           | 13 | .732              | .009              | .025              | .3538       | .4446          |
| 4           | 20 | .881              | .011              | .021              | .3349       | .4558          |
| 5           | 62 | .567              | .007              | .025              | .3371       | .4537          |
| 6           | 13 | .518              | .009              | .026              | .3563       | .4434          |
| 7           | 53 | .109              | .006              | .037              | .3508       | .4519          |
| 8           | 26 | .384              | .010              | .028              | .3542       | .4447          |
| 9           | 24 | 1.048             | .007              | .020              | .3556       | .4413          |
| 10          | 41 | 1.218             | .007              | .017              | .3512       | .4429          |
| 11          | 50 | .834              | .009              | .019              | .3508       | .4447          |
| 12          | 17 | .765              | .009              | .022              | .3331       | .4560          |
| 13          | 19 | .562              | .007              | .025              | .3266       | .4599          |
| 14          | 21 | .599              | .009              | .028              | .3611       | .4411          |
| 15          | 53 | .690              | .013              | .024              | .3536       | .4463          |
| 16          | 26 | .976              | .009              | .018              | .3562       | .4412          |
| 17          | 48 | 1.488             | .009              | .020              | .3584       | .4389          |
| 18          | 25 | .489              | .009              | .024              | .3423       | .4505          |

**TABLE 11**  
**Nursing—Practical**

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 12 | 1.486             | .010              | .033              | .5169       | .2891          |
| 2                | 11 | .617              | .013              | .034              | .5157       | .2901          |
| 3                | 28 | .533              | .012              | .034              | .5037       | .2965          |
| 4                | 22 | .332              | .015              | .033              | .5035       | .2968          |
| 5                | 14 | .582              | .012              | .035              | .5119       | .2929          |
| 6                | 51 | .339              | .013              | .034              | .5224       | .2864          |
| 7                | 15 | .652              | .012              | .032              | .4942       | .3011          |
| 8                | 33 | .593              | .011              | .033              | .5150       | .2894          |
| 9                | 10 | .535              | .012              | .033              | .5105       | .2925          |
| 10               | 23 | .831              | .011              | .034              | .5101       | .2931          |
| 11               | 57 | .361              | .013              | .031              | .5109       | .2915          |
| 12               | 11 | .408              | .013              | .034              | .5117       | .2923          |
| 13               | 15 | .548              | .012              | .033              | .5152       | .2900          |
| 14               | 19 | .349              | .014              | .035              | .5085       | .2956          |
| 15               | 37 | .649              | .015              | .035              | .5186       | .2905          |
| 16               | 16 | 1.068             | .011              | .034              | .5114       | .2925          |
| 17               | 59 | .546              | .011              | .033              | .5228       | .2855          |
| 18               | 16 | .409              | .014              | .034              | .5162       | .2902          |
| 19               | 26 | .777              | .013              | .034              | .5189       | .2887          |

**TABLE 12**  
**Other Health**

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 11 | -1.613            | .036              | .041              | .5000       | .3845          |
| 2                | 23 | .191              | .018              | .031              | .5081       | .3728          |
| 3                | 89 | .202              | .013              | .031              | .4864       | .3850          |
| 4                | 62 | 1.331             | .000              | .028              | .5008       | .3737          |
| 5                | 10 | .070              | .019              | .032              | .5012       | .3770          |
| 6                | 10 | .467              | .013              | .031              | .4975       | .3787          |
| 7                | 90 | .756              | .013              | .026              | .4957       | .3763          |
| 8                | 21 | .718              | .014              | .029              | .5038       | .3747          |
| 9                | 21 | 1.551             | .008              | .023              | .5003       | .3764          |
| 10               | 33 | -1.694            | .029              | .043              | .5012       | .3802          |
| 11               | 15 | -1.064            | .028              | .038              | .5073       | .3737          |
| 12               | 16 | .913              | .011              | .027              | .5006       | .3763          |
| 13               | 51 | 1.052             | .005              | .027              | .5000       | .3738          |
| 14               | 10 | .204              | .021              | .033              | .5000       | .3779          |
| 15               | 14 | 1.570             | .007              | .024              | .5035       | .3732          |
| 16               | 53 | .832              | .023              | .039              | .4964       | .3846          |

**TABLE 13**  
**Accounting**

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 10 | .236              | .022              | .023              | .5190       | .4011          |
| 2                | 17 | .282              | .021              | .035              | .5223       | .3984          |
| 3                | 10 | .250              | .021              | .027              | .5231       | .3968          |
| 4                | 32 | .599              | .024              | .039              | .5281       | .3970          |
| 5                | 21 | .502              | .019              | .021              | .5203       | .3968          |
| 6                | 20 | .608              | .024              | .041              | .5279       | .3973          |
| 7                | 20 | .578              | .020              | .021              | .5138       | .4069          |
| 8                | 24 | 1.189             | .018              | .012              | .5199       | .3982          |
| 9                | 36 | .339              | .022              | .028              | .5128       | .4070          |
| 10               | 10 | .090              | .021              | .031              | .5222       | .3971          |
| 11               | 30 | .226              | .022              | .035              | .5239       | .3971          |
| 12               | 14 | .145              | .020              | .028              | .5226       | .3968          |
| 13               | 33 | .800              | .020              | .021              | .5217       | .3965          |
| 14               | 14 | .507              | .019              | .022              | .5221       | .3973          |

**TABLE 14**  
**Business Administration (4-year transfer)**

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 53 | .418              | .016              | .018              | .2679       | .4308          |
| 2                | 30 | .279              | .018              | .021              | .3352       | .4047          |
| 3                | 26 | .394              | .017              | .024              | .3397       | .4042          |
| 4                | 15 | .602              | .014              | .020              | .3322       | .4046          |
| 5                | 15 | .586              | .012              | .019              | .3232       | .4080          |
| 6                | 11 | .437              | .016              | .022              | .3339       | .4050          |
| 7                | 66 | .921              | .016              | .016              | .3026       | .4160          |
| 8                | 19 | .421              | .015              | .020              | .3322       | .4049          |
| 9                | 12 | .422              | .016              | .021              | .3405       | .4017          |
| 10               | 11 | .335              | .016              | .022              | .3293       | .4070          |
| 11               | 16 | .339              | .017              | .022              | .3400       | .4026          |
| 12               | 32 | .461              | .016              | .020              | .3327       | .4049          |

**TABLE 15**  
**Computer Programming**

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_3$ | $\tilde{\beta}_5$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 10 | -.138             | .020              | .034              | .4498       | .5378          |
| 2           | 13 | -.360             | .020              | .033              | .4377       | .5496          |
| 3           | 10 | -.491             | .020              | .034              | .4411       | .5454          |
| 4           | 37 | .377              | .016              | .033              | .4494       | .5351          |
| 5           | 23 | -.330             | .020              | .035              | .4477       | .5417          |
| 6           | 12 | -1.193            | .023              | .039              | .4432       | .5527          |
| 7           | 55 | -.758             | .023              | .036              | .4504       | .5326          |
| 8           | 20 | -.685             | .021              | .036              | .4460       | .5448          |
| 9           | 16 | .564              | .015              | .034              | .4519       | .5344          |
| 10          | 12 | -.376             | .018              | .037              | .4483       | .5408          |
| 11          | 40 | -.825             | .021              | .036              | .4469       | .5417          |
| 12          | 10 | -.599             | .020              | .035              | .4455       | .5409          |

**TABLE 16**  
**Data Processing**

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 12 | -.382             | .028              | .034              | .5082       | .4715          |
| 2           | 12 | .006              | .029              | .032              | .5015       | .4788          |
| 3           | 14 | .495              | .019              | .025              | .5016       | .4760          |
| 4           | 18 | .072              | .020              | .027              | .4977       | .4801          |
| 5           | 12 | -.528             | .027              | .036              | .5081       | .4735          |
| 6           | 15 | -.151             | .027              | .032              | .5028       | .4788          |
| 7           | 19 | .040              | .022              | .028              | .4979       | .4794          |
| 8           | 10 | -1.144            | .018              | .041              | .5054       | .4765          |
| 9           | 10 | -.699             | .023              | .039              | .5034       | .4787          |
| 10          | 10 | -.696             | .022              | .039              | .5066       | .4747          |
| 11          | 30 | -.881             | .031              | .038              | .4860       | .4963          |
| 12          | 35 | -.857             | .035              | .037              | .5107       | .4757          |
| 13          | 28 | .873              | .028              | .036              | .4966       | .4875          |
| 14          | 50 | -1.004            | .026              | .043              | .5009       | .4872          |
| 15          | 12 | -.757             | .028              | .036              | .5044       | .4766          |
| 16          | 17 | -.661             | .020              | .035              | .5024       | .4784          |
| 17          | 37 | -.790             | .023              | .041              | .4935       | .4898          |
| 18          | 17 | -.908             | .025              | .037              | .5045       | .4767          |

**TABLE 17**  
**Secretarial Science**

| Institution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1           | 22 | .618              | .020              | .031              | .4678       | .4798          |
| 2           | 44 | .085              | .018              | .029              | .4648       | .4831          |
| 3           | 49 | -.134             | .019              | .029              | .4691       | .4814          |
| 4           | 40 | .319              | .020              | .031              | .4622       | .4877          |
| 5           | 27 | .004              | .017              | .026              | .4602       | .4868          |
| 6           | 48 | .162              | .018              | .029              | .4621       | .4849          |
| 7           | 64 | .089              | .023              | .032              | .4768       | .4786          |
| 8           | 33 | .128              | .020              | .030              | .4662       | .4839          |
| 9           | 23 | .176              | .020              | .029              | .4567       | .4921          |
| 10          | 34 | .084              | .017              | .027              | .4586       | .4873          |
| 11          | 24 | .207              | .019              | .028              | .4636       | .4836          |
| 12          | 25 | .142              | .020              | .030              | .4609       | .4898          |
| 13          | 23 | .121              | .019              | .029              | .4654       | .4824          |
| 14          | 31 | .059              | .020              | .029              | .5215       | .4770          |
| 15          | 30 | .121              | .019              | .028              | .4585       | .4910          |
| 16          | 40 | .161              | .019              | .031              | .4549       | .4977          |
| 17          | 21 | .445              | .020              | .030              | .4664       | .4816          |
| 18          | 32 | -.030             | .021              | .029              | .4602       | .4928          |
| 19          | 36 | -.101             | .021              | .031              | .4768       | .4799          |
| 20          | 51 | .151              | .020              | .029              | .4693       | .4807          |
| 21          | 32 | .063              | .019              | .027              | .4517       | .4959          |
| 22          | 33 | .323              | .018              | .027              | .4545       | .4898          |
| 23          | 35 | .248              | .022              | .033              | .4716       | .4840          |
| 24          | 42 | .100              | .020              | .029              | .4764       | .4776          |
| 25          | 46 | .271              | .019              | .030              | .4616       | .4879          |
| 26          | 29 | .036              | .020              | .030              | .4698       | .4819          |

**TABLE 18**  
**Electrical Engineering Technology**

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_5$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 17 | - .337            | .012              | .031              | .011              | .4535       | .5977          |
| 2                | 25 | - .308            | .013              | .031              | .010              | .4511       | .6016          |
| 3                | 21 | - .457            | .012              | .031              | .012              | .4371       | .6130          |
| 4                | 57 | .174              | .011              | .029              | .010              | .4491       | .5890          |
| 5                | 16 | - .541            | .012              | .032              | .012              | .4451       | .6052          |
| 6                | 39 | -1.065            | .018              | .033              | .013              | .4550       | .6032          |
| 7                | 28 | - .429            | .012              | .031              | .011              | .4484       | .5984          |
| 8                | 18 | -1.257            | .018              | .034              | .013              | .4362       | .6289          |
| 9                | 15 | - .430            | .013              | .031              | .011              | .4489       | .6018          |
| 10               | 28 | - .707            | .013              | .032              | .013              | .4328       | .6284          |
| 11               | 45 | - .679            | .015              | .031              | .013              | .4475       | .6094          |
| 12               | 15 | - .487            | .013              | .031              | .011              | .4506       | .5995          |
| 13               | 15 | - .338            | .011              | .031              | .011              | .4501       | .5991          |
| 14               | 34 | - .796            | .012              | .033              | .013              | .4412       | .6151          |
| 15               | 17 | - .884            | .014              | .032              | .012              | .4432       | .6086          |
| 16               | 17 | - .098            | .011              | .030              | .011              | .4483       | .5990          |
| 17               | 17 | - .501            | .014              | .031              | .011              | .4513       | .5987          |
| 18               | 65 | - .483            | .014              | .031              | .012              | .4648       | .5824          |
| 19               | 15 | .328              | .009              | .029              | .010              | .4476       | .6011          |
| 20               | 72 | .037              | .009              | .029              | .010              | .4577       | .5820          |
| 21               | 26 | .184              | .009              | .028              | .010              | .4462       | .5976          |
| 22               | 18 | - .271            | .010              | .030              | .010              | .4354       | .6115          |
| 23               | 29 | .112              | .010              | .029              | .010              | .4354       | .6209          |
| 24               | 59 | -1.421            | .019              | .034              | .015              | .4456       | .6254          |
| 25               | 25 | -1.001            | .013              | .033              | .013              | .4304       | .6293          |
| 26               | 70 | - .622            | .013              | .032              | .012              | .4388       | .6129          |
| 27               | 21 | - .785            | .014              | .032              | .012              | .4409       | .6096          |

TABLE 19

## Science (4-year transfer)

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_5$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 40 | .281              | .023              | .011              | .4414       | .4588          |
| 2                | 16 | -.283             | .031              | .014              | .4549       | .4496          |
| 3                | 14 | .681              | .017              | .020              | .4569       | .4462          |
| 4                | 11 | .425              | .026              | .005              | .4534       | .4486          |
| 5                | 15 | .281              | .024              | .012              | .4544       | .4474          |
| 6                | 58 | 2.054             | .009              | .000              | .4400       | .4557          |
| 7                | 24 | -.101             | .030              | .011              | .4563       | .4475          |
| 8                | 12 | .515              | .026              | .001              | .4522       | .4494          |
| 9                | 13 | .751              | .019              | .015              | .4551       | .4474          |
| 10               | 32 | .658              | .019              | .017              | .4586       | .4430          |

TABLE 20

## Other Technical

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_5$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------|----------------|
| 1                | 10 | .825              | .030              | .3626       | .4513          |
| 2                | 13 | .922              | .031              | .3754       | .4437          |
| 3                | 20 | .759              | .033              | .3776       | .4432          |
| 4                | 20 | 1.496             | .029              | .3794       | .4401          |
| 5                | 14 | 1.722             | .029              | .3778       | .4422          |
| 6                | 12 | .434              | .033              | .3724       | .4460          |
| 7                | 11 | .913              | .031              | .3754       | .4431          |
| 8                | 12 | .677              | .033              | .3722       | .4470          |
| 9                | 41 | .976              | .031              | .3728       | .4456          |
| 10               | 15 | 1.006             | .030              | .3700       | .4461          |
| 11               | 23 | .931              | .031              | .3728       | .4442          |
| 12               | 16 | .755              | .033              | .3706       | .4489          |
| 13               | 17 | .433              | .033              | .3705       | .4477          |
| 14               | 10 | 1.195             | .031              | .3736       | .4453          |
| 15               | 19 | .768              | .031              | .3765       | .4421          |
| 16               | 33 | 1.651             | .029              | .3700       | .4466          |
| 17               | 35 | .590              | .034              | .3774       | .4447          |
| 18               | 25 | 1.502             | .029              | .3807       | .4396          |
| 19               | 23 | .805              | .032              | .3718       | .4470          |

TABLE 21

## Auto Mechanics

| Insti-<br>tution | N   | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|-----|-------------------|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 18  | .159              | .015              | .013              | .018              | .4160       | .4369          |
| 2                | 16  | .261              | .015              | .014              | .016              | .4211       | .4336          |
| 3                | 15  | -.159             | .015              | .013              | .021              | .4196       | .4340          |
| 4                | 28  | 1.475             | .013              | .012              | .001              | .4170       | .4353          |
| 5                | 38  | .926              | .013              | .013              | .007              | .3935       | .4504          |
| 6                | 64  | .125              | .016              | .013              | .016              | .4260       | .4300          |
| 7                | 41  | 1.208             | .013              | .010              | .005              | .4167       | .4320          |
| 8                | 15  | .166              | .012              | .012              | .019              | .4066       | .4413          |
| 9                | 19  | 1.602             | .013              | .011              | .001              | .4184       | .4345          |
| 10               | 34  | .571              | .014              | .012              | .013              | .4114       | .4384          |
| 11               | 38  | .155              | .018              | .015              | .015              | .4259       | .4339          |
| 12               | 39  | .389              | .014              | .013              | .016              | .4283       | .4268          |
| 13               | 174 | .249              | .011              | .015              | .018              | .4471       | .4129          |
| 14               | 23  | .944              | .014              | .012              | .009              | .4242       | .4297          |
| 15               | 16  | .570              | .014              | .012              | .013              | .4219       | .4311          |
| 16               | 37  | -.107             | .015              | .012              | .022              | .3911       | .4553          |
| 17               | 16  | .227              | .015              | .013              | .017              | .4068       | .4445          |
| 18               | 20  | -.263             | .015              | .013              | .023              | .4205       | .4342          |
| 19               | 96  | .165              | .018              | .012              | .015              | .3981       | .4505          |
| 20               | 17  | 1.401             | .013              | .012              | .002              | .4123       | .4382          |



TABLE 22

## Drafting

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 68 | -.655             | .026              | .024              | .009              | .4468       | .5158          |
| 2                | 10 | -.274             | .025              | .015              | .015              | .4497       | .5104          |
| 3                | 30 | .331              | .023              | .018              | .009              | .4584       | .5024          |
| 4                | 10 | -.279             | .025              | .018              | .013              | .4481       | .5104          |
| 5                | 26 | -.173             | .025              | .014              | .012              | .4528       | .5058          |
| 6                | 25 | -.392             | .024              | .016              | .013              | .4463       | .5115          |
| 7                | 11 | -.668             | .026              | .013              | .016              | .4432       | .5175          |
| 8                | 10 | -.389             | .025              | .016              | .014              | .4504       | .5068          |
| 9                | 11 | -.758             | .025              | .018              | .016              | .4521       | .5077          |
| 10               | 15 | -.475             | .024              | .017              | .013              | .4380       | .5195          |
| 11               | 17 | -.027             | .023              | .019              | .004              | .4378       | .5197          |
| 12               | 62 | -.514             | .023              | .023              | .013              | .4591       | .4987          |
| 13               | 12 | -.528             | .026              | .020              | .011              | .4410       | .5199          |
| 14               | 10 | -.763             | .027              | .015              | .018              | .4396       | .5225          |
| 15               | 11 | .157              | .025              | .016              | .008              | .4491       | .5095          |
| 16               | 74 | -.594             | .026              | .016              | .019              | .4430       | .5188          |
| 17               | 26 | .202              | .022              | .017              | .000              | .4398       | .5158          |

TABLE 23

## Machine Work

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_4$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 12 | -.173             | .024              | .035              | .5900       | .3855          |
| 2                | 14 | .613              | .005              | .039              | .5931       | .3822          |
| 3                | 24 | .139              | .004              | .038              | .5925       | .3793          |
| 4                | 10 | -.573             | .032              | .036              | .5964       | .3810          |
| 5                | 12 | -.703             | .021              | .038              | .5941       | .3803          |
| 6                | 17 | -.886             | .033              | .035              | .5954       | .3785          |
| 7                | 27 | -.089             | .021              | .033              | .5906       | .3817          |
| 8                | 19 | -1.444            | .043              | .033              | .5931       | .3823          |
| 9                | 11 | -.307             | .010              | .040              | .5920       | .3835          |
| 10               | 17 | .067              | .006              | .039              | .5891       | .3862          |

TABLE 24

## Other Trades

| Insti-<br>tution | N   | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_4$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|-----|-------------------|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 90  | 1.283             | .012              | .006              | .007              | .3794       | .4783          |
| 2                | 34  | .595              | .017              | .009              | .013              | .4154       | .4854          |
| 3                | 29  | .599              | .015              | .011              | .012              | .3916       | .4782          |
| 4                | 67  | 1.052             | .019              | .008              | .007              | .3828       | .4844          |
| 5                | 40  | .713              | .013              | .010              | .011              | .3774       | .4882          |
| 6                | 49  | 1.279             | .016              | .006              | .006              | .3798       | .4839          |
| 7                | 54  | .688              | .018              | .010              | .010              | .3830       | .4871          |
| 8                | 28  | .845              | .015              | .009              | .010              | .3926       | .4885          |
| 9                | 31  | .487              | .018              | .011              | .012              | .3624       | .5040          |
| 10               | 58  | .615              | .016              | .011              | .011              | .3605       | .5022          |
| 11               | 27  | .682              | .016              | .009              | .011              | .3840       | .4845          |
| 12               | 21  | 1.227             | .018              | .005              | .006              | .3753       | .4894          |
| 13               | 25  | .789              | .016              | .009              | .010              | .3556       | .5045          |
| 14               | 20  | .507              | .016              | .012              | .012              | .3810       | .4883          |
| 15               | 138 | .900              | .014              | .008              | .010              | .3820       | .4764          |
| 16               | 194 | .571              | .013              | .010              | .014              | .4023       | .4696          |
| 17               | 39  | 1.061             | .019              | .007              | .007              | .3823       | .4867          |
| 18               | 47  | .703              | .018              | .009              | .011              | .3742       | .4918          |
| 19               | 37  | 1.035             | .018              | .008              | .008              | .3750       | .4899          |
| 20               | 34  | .692              | .018              | .009              | .011              | .3863       | .4827          |
| 21               | 51  | .462              | .017              | .011              | .013              | .3733       | .4942          |
| 22               | 60  | .799              | .016              | .009              | .010              | .3773       | .4894          |
| 23               | 167 | .340              | .016              | .013              | .014              | .3408       | .5264          |
| 24               | 58  | .767              | .011              | .009              | .012              | .3556       | .5017          |

TABLE 25

## Cosmetology

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------|----------------|
| 1                | 15 | 1.716             | .032              | .5365       | .1002          |
| 2                | 33 | 1.473             | .030              | .4466       | .6277          |
| 3                | 17 | 1.419             | .016              | .3111       | .1373          |
| 4                | 15 | 1.702             | .034              | .5830       | .1505          |
| 5                | 18 | 1.463             | .023              | .2391       | .6039          |
| 6                | 15 | 1.490             | .023              | .0000       | .9227          |
| 7                | 12 | 1.359             | .016              | .4441       | .0932          |
| 8                | 16 | 1.506             | .026              | .3319       | .2867          |
| 9                | 22 | 1.541             | .033              | .5046       | .5539          |

TABLE 26

## Police Science

| Insti-<br>tution | N  | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|------------------|----|-------------------|-------------------|-------------------|-------------|----------------|
| 1                | 51 | .462              | .015              | .025              | .4221       | .4716          |
| 2                | 18 | .561              | .013              | .025              | .4290       | .4642          |
| 3                | 36 | 1.312             | .009              | .018              | .4171       | .4721          |
| 4                | 26 | .732              | .015              | .021              | .4211       | .4702          |
| 5                | 18 | .609              | .014              | .022              | .4242       | .4670          |
| 6                | 24 | .821              | .013              | .023              | .4280       | .4647          |
| 7                | 21 | 1.621             | .007              | .020              | .4261       | .4666          |
| 8                | 15 | .226              | .018              | .028              | .4317       | .4634          |

**TABLE 27**  
**Social Science (4-year transfer)**

| Institution | N   | $\tilde{\beta}_0$ | $\tilde{\beta}_7$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|-----|-------------------|-------------------|-------------|----------------|
| 1           | 69  | .910              | .026              | .0000       | .5724          |
| 2           | 31  | 1.286             | .021              | .1555       | .5449          |
| 3           | 20  | 1.409             | .020              | .1652       | .5420          |
| 4           | 18  | 1.647             | .018              | .1545       | .5447          |
| 5           | 152 | 2.296             | .010              | .1462       | .5456          |
| 6           | 30  | .867              | .026              | .1732       | .5405          |
| 7           | 37  | .825              | .027              | .1212       | .5570          |
| 8           | 17  | 1.173             | .023              | .1700       | .5412          |
| 9           | 16  | 1.441             | .020              | .1584       | .5448          |
| 10          | 19  | 1.650             | .018              | .1714       | .5397          |
| 11          | 10  | 1.475             | .020              | .1596       | .5431          |

**TABLE 28**  
**Arts and Humanities (4-year transfer)**

| Institution | N   | $\tilde{\beta}_0$ | $\tilde{\beta}_1$ | $\tilde{R}$ | $\tilde{\phi}$ |
|-------------|-----|-------------------|-------------------|-------------|----------------|
| 1           | 25  | 1.730             | .015              | .0900       | .5577          |
| 2           | 17  | 1.889             | .015              | .1352       | .5497          |
| 3           | 236 | 2.067             | .011              | .0000       | .5760          |
| 4           | 15  | 1.289             | .022              | .1685       | .5416          |
| 5           | 22  | 1.492             | .019              | .1545       | .5454          |
| 6           | 11  | .873              | .026              | .1371       | .5501          |

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